Angle-resolved photoemission observation of isotropic superconducting gaps in isovalent Ru-substituted $Ba(Fe_{0.75}Ru_{0.25})_2As_2$

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We used high-energy resolution angle-resolved photoemission spectroscopy to extract the momentum dependence of the superconducting gap of Ru-substituted Ba(Fe_{0.75}Ru_{0.25})₂As₂ (T_c = 15 K). Despite a strong out-of-plane warping of the Fermi surface, the magnitude of the superconducting gap observed experimentally is nearly isotropic and independent of the out-of-plane momentum. More precisely, we respectively observed 5.7 and 4.5 meV superconducting gaps on the inner and outer Γ -centered hole Fermi surface pockets, whereas a 4.8 meV gap is recorded on the M-centered electron Fermi surface pockets. Our results are consistent with the J_1 - J_2 model with a dominant antiferromagnetic exchange interaction between the next-nearest Fe neighbors.

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The mechanism for Cooper pairing is the most important issue in high- T_c superconductivity. Due to its momentum resolution capabilities, angle-resolved photoemission spectroscopy (ARPES) is a very powerful tool to investigate the superconducting (SC) gap size and symmetry directly in momentum space. Previous ARPES experiments revealed Fermisurface (FS) -dependent and nearly isotropic SC gaps for both hole-doped¹⁻⁵ and electron-doped⁶ 122-ferropnictides. In contrast, a circular horizontal node at $k_z = \pi$ was recently reported on a hole FS pocket with strong three-dimensional (3D) character in isovalent P-substituted BaFe₂(As_{0.7}P_{0.3})₂.⁷ Whether such a feature is unique or common to other isovalently substituted BaFe₂As₂ materials is still under intense debate. Ba($Fe_{1-x}Ru_x$)₂As₂ is another isovalent substituted system with maximum critical temperatures T_c around 20 K.^{8–11} As with BaFe₂(As_{0.7}P_{0.3})₂, previous ARPES studies of the electronic band structure indicate that this system exhibits a pronounced 3D character, 12-14 thus raising the possibility of SC gap nodes. Indeed, recent measurements of a finite residual thermal conductivity suggest the presence of nodes. Unfortunately, samples of Ba($Fe_{1-x}Ru_x$)₂As₂ usually show only a partial SC volume fraction detrimental to a determination of the momentum-resolved SC gap by ARPES.

In this paper, we report high-energy resolution ARPES results on SC Ba(Fe_{0.75}Ru_{0.25})₂As₂ ($T_c = 15$ K) recorded in the whole 3D Brillouin zone (BZ) by tuning the incident photon energy ($h\nu$). Due to improved sample quality, we observed the opening of a SC gap. We demonstrate that the SC gap size at this doping level is nearly isotropic on each FS, and slightly FS-dependent. Interestingly, the global gap structure in this material can be described by a single gap function derived from a strong-coupling approach.

Large single crystals of Ba(Fe_{0.75}Ru_{0.25})₂As₂ were grown by the self-flux method. ¹¹ ARPES measurements were performed at the 1-cubed ARPES end-station of BESSY and at Swiss Light Source beamline SIS using a VG-Scienta R4000 electron analyzer with $h\nu$ ranging from 22 to 64 eV, and at Tohoku University using a VG-Scienta SES2002 electron analyzer with a He discharge lamp ($h\nu = 21.218$ eV). The angular resolution was set to 0.2° and the energy resolution to 4–7 meV for the SC gap measurements at T=0.9 K in BESSY, and T=6 K in Tohoku University. Clean surfaces for the ARPES measurements were obtained by cleaving crystals $in\ situ$ in a working vacuum better than 5×10^{-11} Torr. We label the momentum values with respect to the 1 Fe/unit cell BZ, and we use c'=c/2 as the distance between two Fe planes.

Figures 1(a) and 1(b) show the temperature dependence of the resistivity and the dc magnetization of a $Ba(Fe_{0.75}Ru_{0.25})_2As_2$ sample, respectively. Both the resistivity and zero-field-cooled magnetization curves indicate an onset of superconductivity at \sim 15 K. Such a T_c value is consistent with the nominal composition of the sample, as indicated in the phase diagram shown in the inset of Fig. 1(a). The resistivity goes down to zero within 2 K whereas the absolute value of the magnetization becomes large and tends to saturate at low temperature, suggesting that superconductivity is established in most of the bulk material. Yet the saturation is not complete and the SC volume fraction is possibly slightly smaller than 100%.

Figures 2(a) and 2(b) show the FS mappings obtained by integrating the ARPES intensity within $E_F \pm 10$ meV recorded with $h\nu = 21.218$ and 34 eV, respectively. In agreement with our previous study on Ru-substituted BaFe₂As₂, ¹⁴ we observed two almost circular hole FS pockets centered

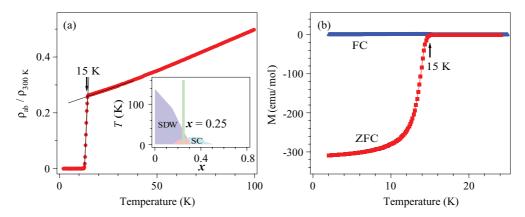


FIG. 1. (Color online) (a) Temperature dependence of the normalized resistivity of $Ba(Fe_{0.75}Ru_{0.25})_2As_2$. Inset: phase diagram of $Ba(Fe_{1-x}Ru_x)_2As_2$. The green bar indicates the composition of the samples measured. (b) Temperature dependence of the dc magnetization of a $Ba(Fe_{0.75}Ru_{0.25})_2As_2$ sample. A dc field of 10 Oe was applied in the measurements in the zero-field-cooling (ZFC) and field-cooling (FC) modes.

at the Γ point, namely α and β , and two elliptical-like electron FS pockets centered at the M point, which hybridize to form the γ and δ FS pockets. From the Fermi wave vector (k_F) positions determined experimentally by fitting the momentum distribution curves (MDCs) with Lorentz functions, which are appended in Figs. 2(a) and 2(b), we can trace the FS of this material. The contrast between the FS sizes obtained at 21.218 and 34 eV is important and suggests a strong out-of-plane momentum k_z dependence. To confirm this effect, we performed ARPES experiments over a wide $h\nu$ range. The corresponding FS mapping of the k_x - k_z plane is displayed in Fig. 2(c), where we converted $h\nu$ into k_z by using the nearly-free-electron approximation 15 and the formula $k_z = \frac{1}{\hbar} \sqrt{2mE_k \cos^2 \theta + V_0}$, where θ is the polar angle, E_k is the kinetic energy of the photoemitted electrons, and where an inner potential V_0 of 15 eV was used. As reported previously, 12-14 the electronic structure of Ru-substituted BaFe₂As₂ compounds exhibits an enhanced 3D character as compared with K-doped and Co-doped samples that is mainly attributed to the more specially extended nature of the Ru 4d orbitals. From Fig. 2(c), we determine that

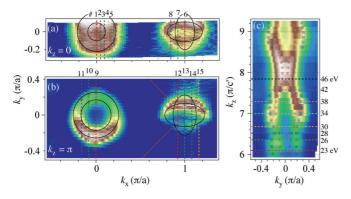


FIG. 2. (Color online) (a) and (b) FS mappings obtained by integrating the ARPES intensity within $E_F \pm 10$ meV at (21.218 eV) $k_z = 0$ and (34 eV) $k_z = \pi$, respectively. The black curves indicate the various FSs. (c) FS mapping in the k_x - k_z plane obtained by tuning $h\nu$. The dashed lines and symbols indicate gap measurement cuts and k_F locations.

 $h\nu = 21.218$ eV is very close to $k_z = 0$ whereas 34 eV corresponds to $k_z = \pi/c'$. We also note that for this relatively low Ru substitution level, the α band crosses the Fermi level (E_F) at all k_z values.

We now turn our attention to the SC gap of Ba(Fe_{0.75}Ru_{0.25})₂As₂. To detect the possible presence of nodes, we recorded high-energy resolution measurements along the various cuts indicated in Fig. 2, which span the whole 3D BZ. The results are summarized in Fig. 3. Following a common practice, all the k_F energy distribution curves (EDCs) have been symmetrized in order to approximately remove the Fermi function cutoff. In Fig. 3(a), we show the temperature evolution of the symmetrized EDC at one k_F location on the α band. At 6 K, the symmetrized EDC spectrum exhibits a peak around 6 meV accompanied by a strong loss of intensity at E_F that characterizes the opening of a SC gap. With temperature increasing, the peak broadens and the SC gap fills in. Both disappear between 13 and 18 K, in agreement with the 15 K SC transition determined for our sample. We display in Fig. 3(b) the temperature dependence of the corresponding gap size.

The symmetrized EDCs recorded at 6 K along the α , β , and γ/δ FSs at $k_z=0$ are shown in Figs. 3(c)–3(e), respectively. As with most of the ARPES measurements on the 122 family of SC ferropnictides, ¹⁶ the SC gap along each FS remains constant within experimental uncertainties. Hence, constant SC gaps of $\Delta_{\alpha}^{k_z=0}=5.7$ meV, $\Delta_{\beta}^{k_z=0}=4.5$ meV, and $\Delta_{\gamma}^{k_z=0}=4.8$ meV are extracted along the α , β , and γ FSs, respectively. Similar results are obtained at 0.9 K for $k_z=\pi$, as shown in Figs. 3(f)–3(h). Indeed, the same SC gap values are found experimentally, and thus $\Delta_{\alpha}^{k_z=\pi}=5.7$ meV, $\Delta_{\beta}^{k_z=\pi}=4.5$ meV, and $\Delta_{\gamma}^{k_z=\pi}=4.8$ meV. These values lead, respectively, to $2\Delta/k_BT_c$ ratios of 9.0, 7.1, and 7.6. Although experimental uncertainties would account for small in-plane anisotropies of the SC gap, our results are inconsistent with the presence of vertical nodes.

To check for the possibility of horizontal nodes, we also performed high-energy resolution ARPES measurements along the warped k_z FS of Ba(Fe_{0.75}Ru_{0.25})₂As₂. The $h\nu$ dependence of the symmetrized EDCs at the k_F positions associated with the α FS is plotted in Fig. 3(i). Despite the

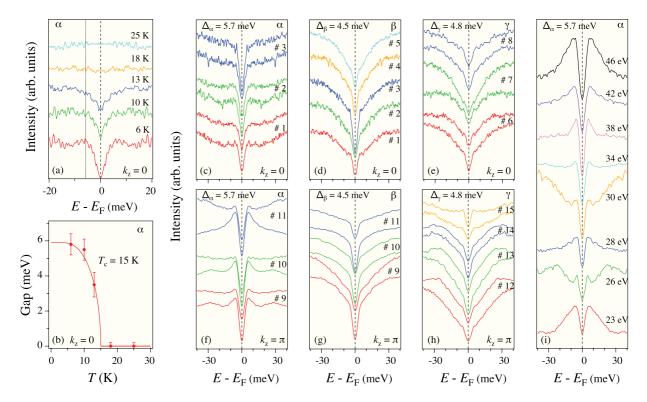


FIG. 3. (Color online) (a) Temperature dependence of the symmetrized EDC spectrum at a k_F point of the α band. (b) Temperature dependence of the measured SC gap on the same band. The red curve corresponds to a fit using the BCS theory. (c)–(e) Symmetrized EDCs in the SC state (6 K) measured at various k_F points in the $k_z=0$ plane along the α , β , and γ/δ FSs, respectively. The labels correspond to the cuts in Figs. 2(a). (f)–(h) Same as (c)–(e) but measured at 0.9 K in the $k_z=\pi$ plane. (i) Symmetrized EDCs in the SC state (0.9 K) measured at various k_F points along the α FS with various $h\nu$ values.

large k_z warping of the α band, our results indicate that the corresponding SC gap is practically constant at all measured $h\nu$ values, suggesting a 3D isotropic SC gap and ruling out the possibility of a horizontal node for this band. In Figs. 4(a) and 4(b), we use the polar representation to illustrate the isotropicity of the SC gap observed for the Γ -centered and M-centered FS pockets, respectively. Even though our ARPES measurements do not allow us to make a conclusive statement about the possibility of a horizontal node for the other bands, the equivalence of the SC gap in the $k_z = 0$ and $k_z = \pi$ planes, which would be the likely possibilities for the occurrence of such a node, strongly suggests that they do not exist. Assuming that samples are not phase-separated, zero-field thermal conductivity is a very sensitive technique to detect the presence of nodes in the SC gap function, and the agreement with ARPES measurements is usually good.¹⁶ A recent thermal conductivity study suggests the presence of nodes in Ba($Fe_{1-x}Ru_x$)₂As₂.¹⁷ Although the phase homogeneity of these materials is usually a matter of concern and one cannot rule out phase separation, the current ARPES study would thus limit the latter observation to accidental nodes at momentum locations that remain undefined.

The nearly isotropic SC gaps observed by ARPES for many Fe-based SC materials¹⁶ have serious implications for the underlying pairing mechanism.¹⁸ In particular, they are inconsistent with the momentum-dependent quasinesting interactions promoted as the driving pairing force in weak-coupling approaches.^{19,20} This is especially true for materials showing a

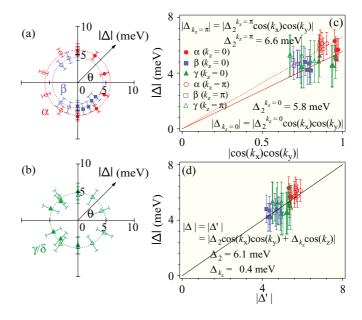


FIG. 4. (Color online) (a),(b) Polar plots of the SC gap size at 6 K for the α , β , and γ/δ FSs as a function of θ . Dashed circles show the averaged SC gap values on each FS. (c) SC gap size as a function of $|\cos k_x \cos k_y|$. The solid and dashed lines represent fits for gap values at $k_z=0$ and $k_z=\pi$, respectively. (d) SC gap size as a function of $|\Delta_2 \cos k_x \cos k_y + \Delta_{k_z} \cos k_z|$ using simultaneously the data for both the $k_z=0$ and $k_z=\pi$ planes.

large FS warping such as Ba(Fe_{0.75}Ru_{0.25})₂As₂. Consequently, instead we analyze our results in the context of the strongcoupling approach and the effective J_1 - J_2 model, ^{21–25} as was done previously for other Fe-based superconductors. 3,5,7,26-32 Assuming that the J_2 parameter characterizing the antiferromagnetic exchange interaction between the next-nearest Fe neighbors dominates in the ferropnictides, ²³ we used a simple SC gap function of the form $|\Delta_2 \cos k_x \cos k_y|$ to fit our data. In Fig. 4(c), we show the results when the $k_z = 0$ and $k_z = \pi$ data are fit independently. Although both sets of data are well fit, they lead to slightly different SC gap parameters $(\Delta_2^{k_z=0}=5.8 \text{ meV} \text{ and } \Delta_2^{k_z=\pi}=6.6 \text{ meV})$. This discrepancy originates from the different size of the FSs in the two different k_z planes. A better agreement is obtained when adding a gap parameter associated with interlayer interactions, as was done previously for Ba_{0.6}K_{0.4}Fe₂As₂. ^{28,29} The result of the simultaneous fit of the two sets of data to the SC gap function $|\Delta_2 \cos k_x \cos k_y + \Delta_{k_z} \cos k_z|$ is displayed in Fig. 4(d). The fit leads to $\Delta_2 = 6.1 \text{ meV}$ and $\Delta_{k_z} = -0.4 \text{ meV}$.

It is quite remarkable that the results obtained on the SC gap of Ba(Fe_{0.75}Ru_{0.25})₂As₂ are not fundamentally different from those reported for its hole-doped and electron-doped SC cousins, which show much weaker FS warping along k_z . Furthermore, they reinforce the assumption that the horizontal node detected in BaFe₂(As_{0.7}P_{0.3})₂, the other major family of the isovalently substituted 122-ferropnictide system, is not enforced by symmetry but rather is accidental.⁷ We caution that in our study the k_F value associated with the α band is always smaller than that corresponding to the other

 Γ -centered hole bands. Our previous study indicates that this is no longer true for the high Ru-substitution side of the phase diagram. ¹⁴ This region could thus be more similar to the BaFe₂(As_{0.7}P_{0.3})₂ system than the samples studied here. Yet, whether accidental horizontal nodes are also possible in this case remains an open question.

In summary, we reported high-energy resolution ARPES results on isovalent Ru-substituted Ba(Fe_{0.75}Ru_{0.25})₂As₂. We observed a nodeless and nearly isotropic SC gap that is slightly FS-sheet-dependent and remains constant at all k_z values. This result indicates that this system is not fundamentally different from the related hole-doped and electron-doped 122 ferropnictide systems, thus pushing toward a rather universal picture for the Fe-based SC materials where the pairing interactions are essentially short-ranged.

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